

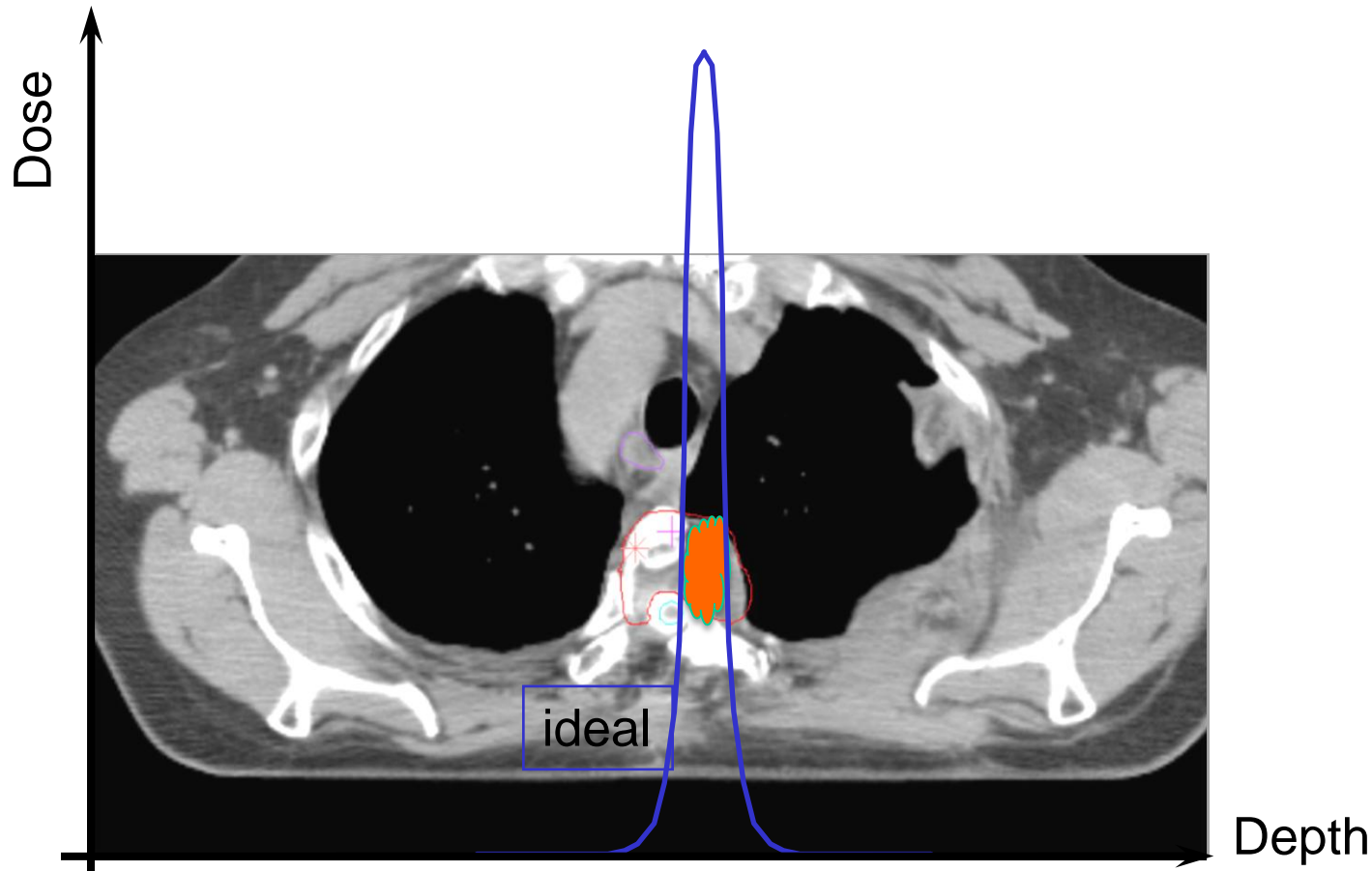


# Physics of particles

**H. Paganetti PhD**

Massachusetts General Hospital & Harvard Medical School

## The ideal dose distribution



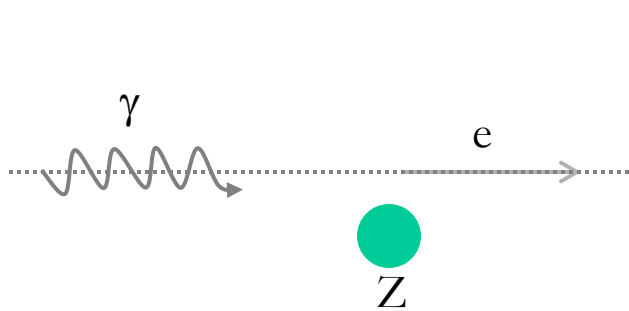
**Dose:** Energy deposited    Energy/Mass    [J/kg] [Gy]



# Introduction

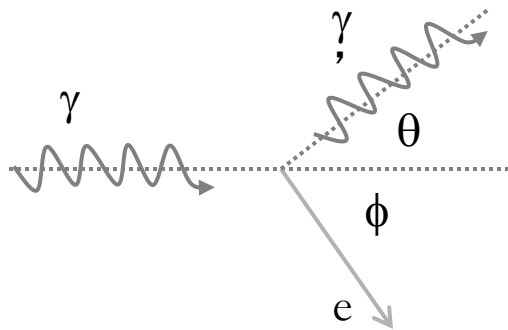
## Photoelectric Effect

Photon ejects electron from an atom.



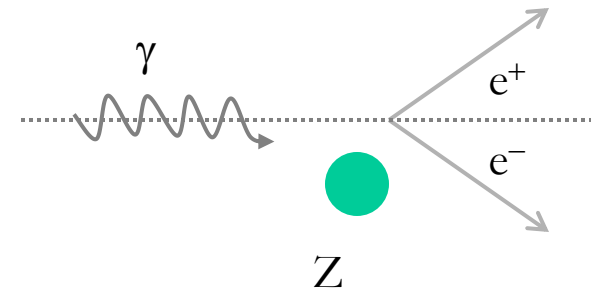
## Compton Effect

Photons scattering from atomic electrons.



## Pair Production

Photons above twice the electron rest mass energy can create an electron positron pair.



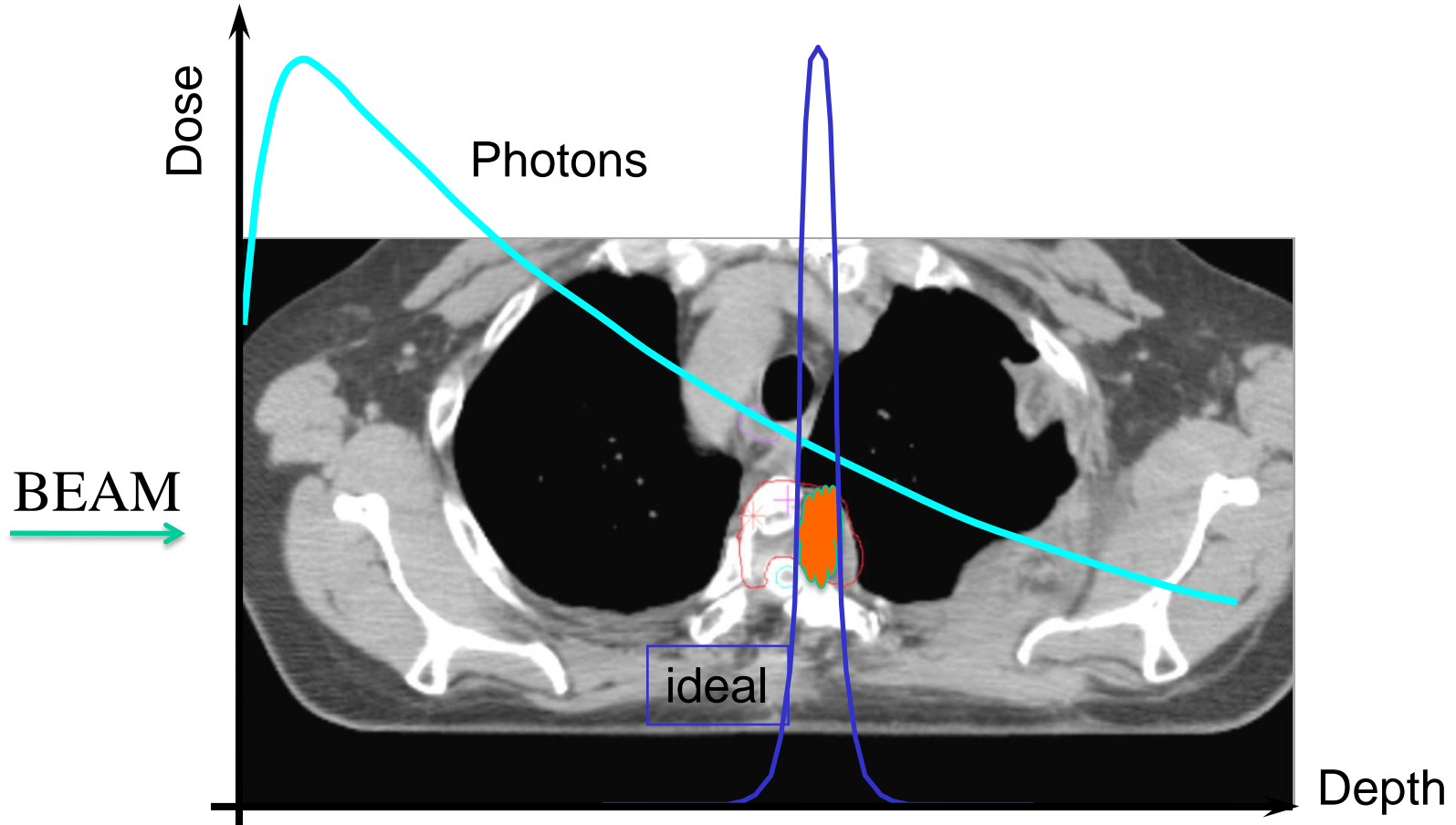
## Dose deposition



Electrons

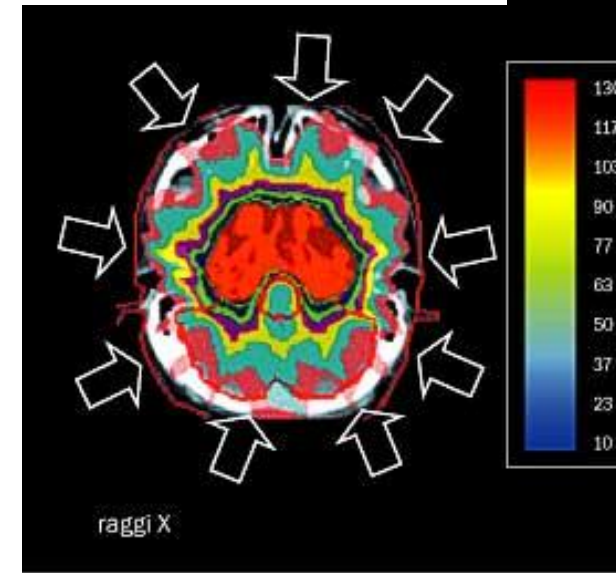
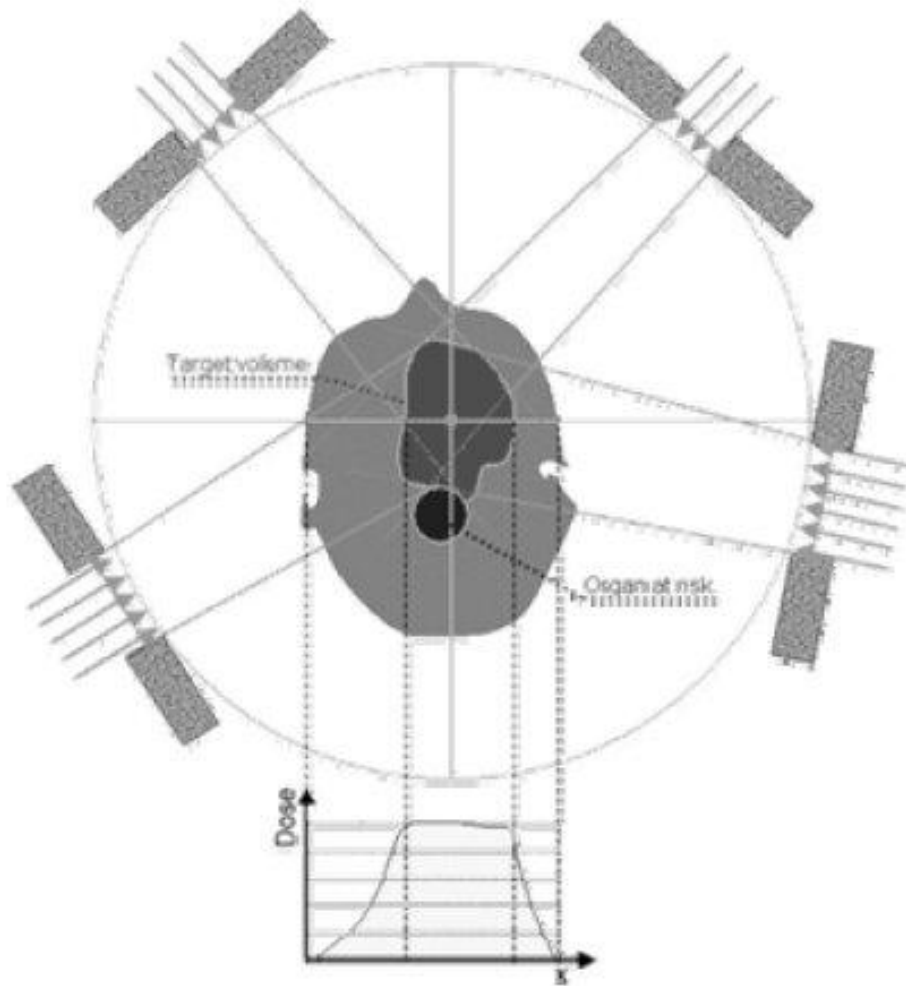


# Introduction



# Introduction

## Use of multiple beams (different directions)



**Also:  
Modulation of intensities**

© INFN



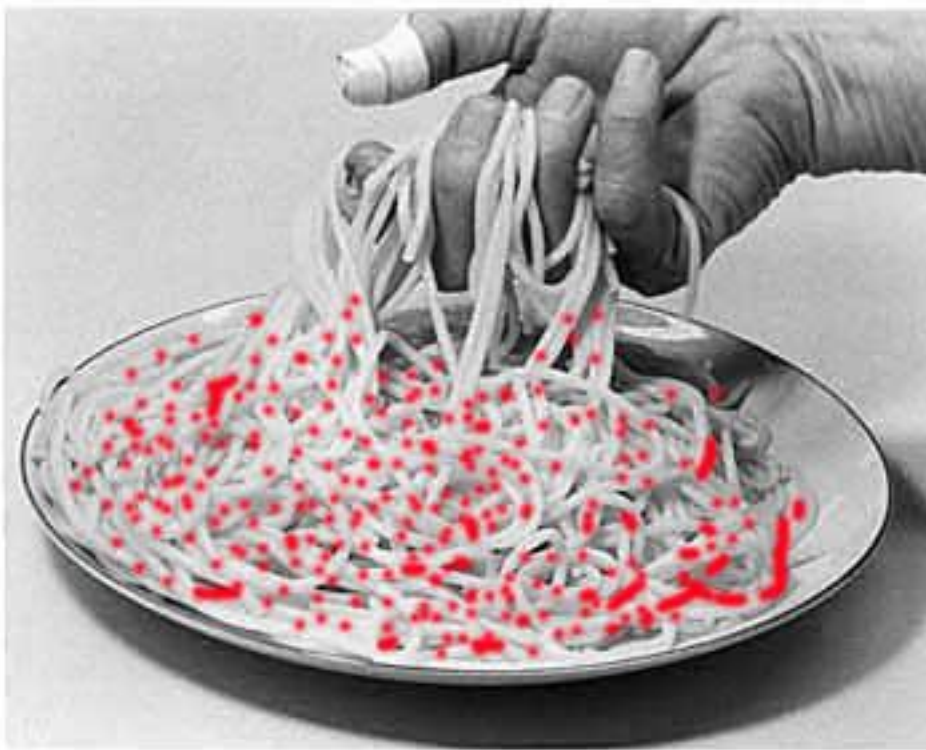
# Introduction

- Photons
  - Charge: 0
  - Indirect Ionization
- Electrons
  - Charge: -1
  - Direct Ionization
  - Mass: 512 keV
- Protons
  - Charge: +1
  - Direct Ionization
  - Mass: 2,000 •  $m_e$

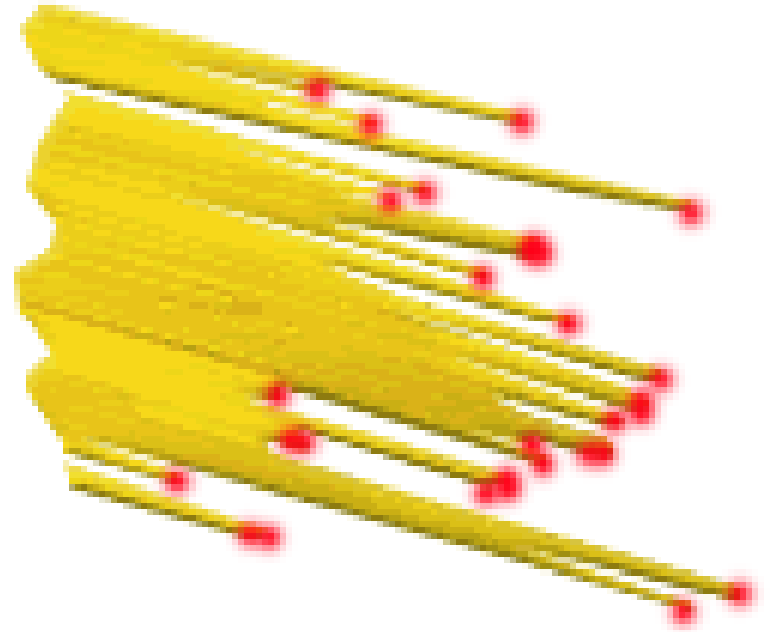




## Dose deposition



Electrons

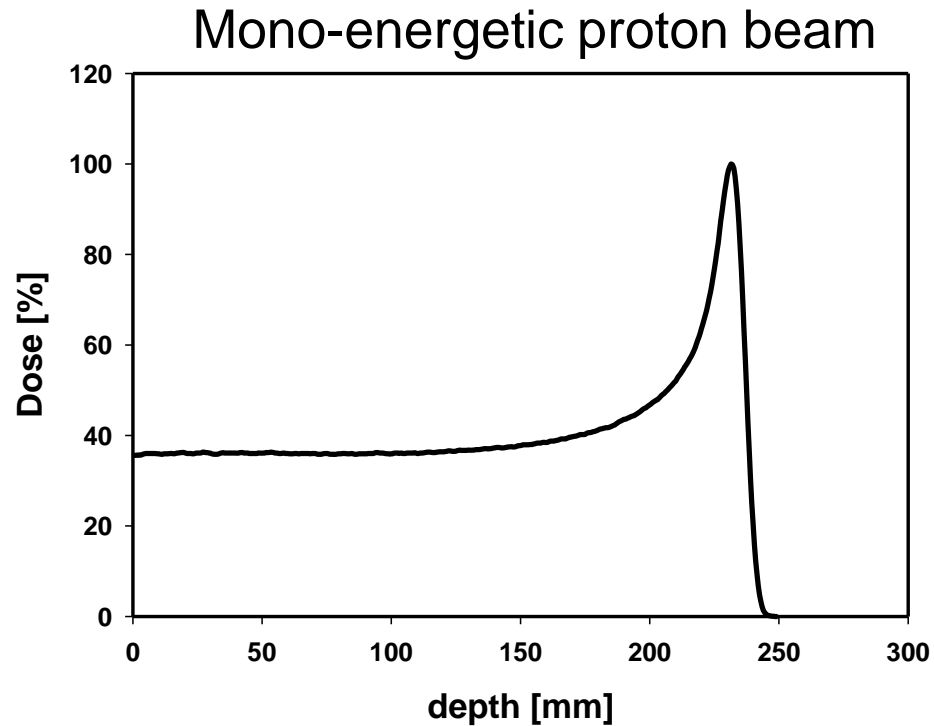


Protons

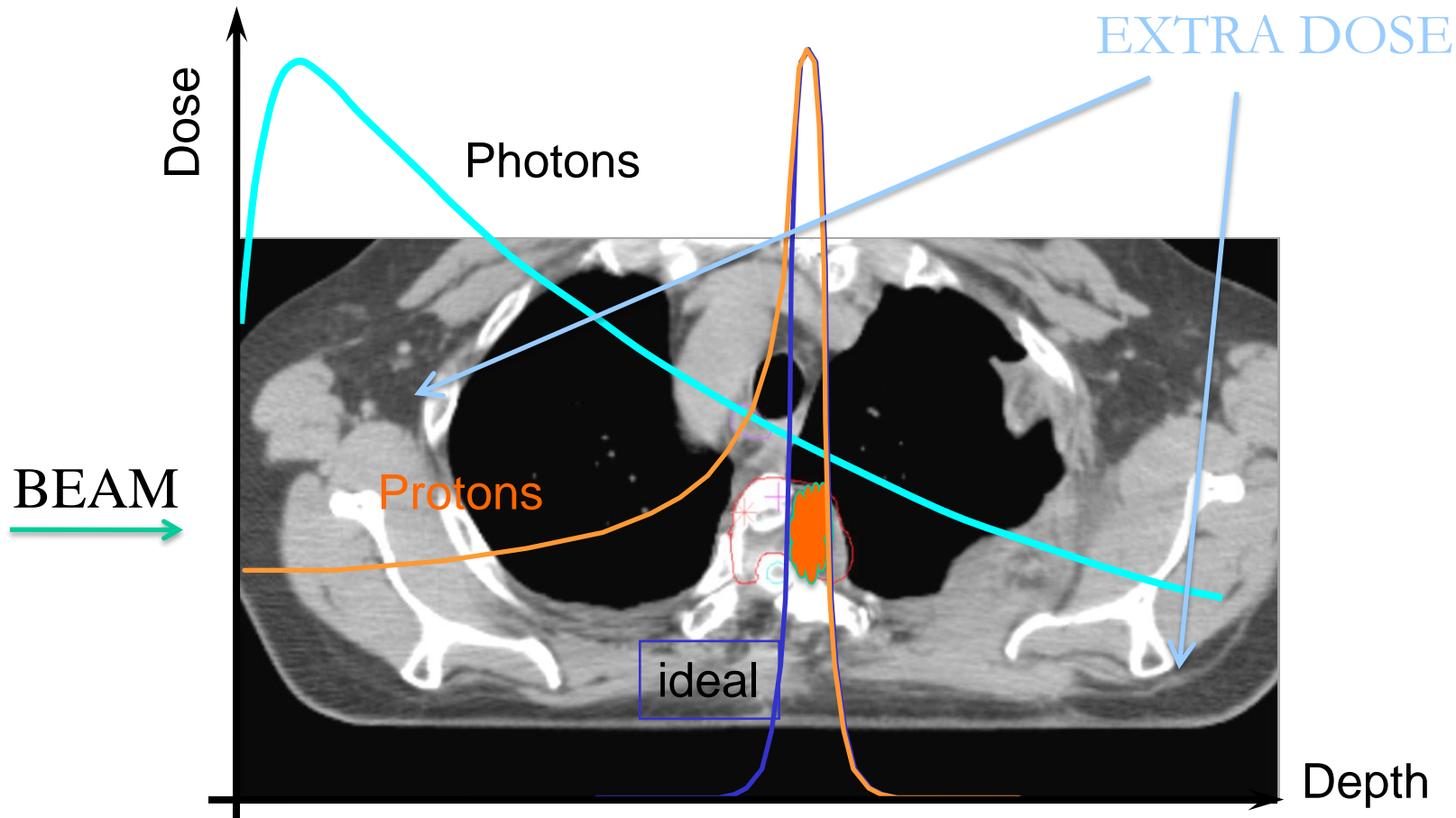




## The Bragg curve



# Introduction

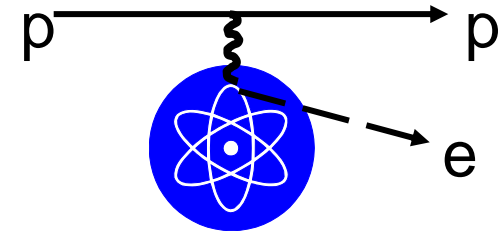


Beam energy controls the range



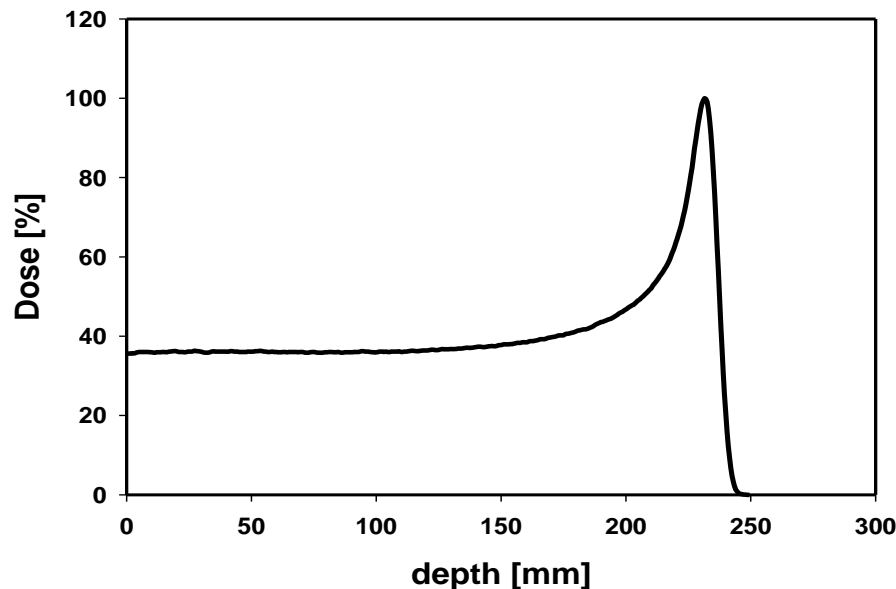
## Electromagnetic energy loss of protons

- Distal distribution



–Ionization

–Excitation



Interaction probability  
is proportional to  
proton energy

## Bethe-Bloch equation

$$\left(\frac{dE}{dx}\right)_0 = \frac{2\pi n_e r_e^2 m_e c^2 z^2}{\beta^2} \left[ \ln\left(\frac{2m_e c^2 \beta^2 T_{\max}}{I^2 (1-\beta^2)}\right) - 2\beta^2 + 2zL_1(\beta) + 2z^2L_2(\beta) - 2\frac{C}{Z} - \delta + G \right]$$

- $I$  : mean excitation energy , material-dependent
- $\delta$  : density correction
- $C$  : is the shell correction, important at low energies
- $T_{\max}$  : maximum energy transfer to an electron
- $L_1$  : Barkas correction ( $z^3$ )
- $L_2$  : Bloch ( $z^4$ ) correction
- $G$  : Mott corrections



## Bethe [-Bloch] equation

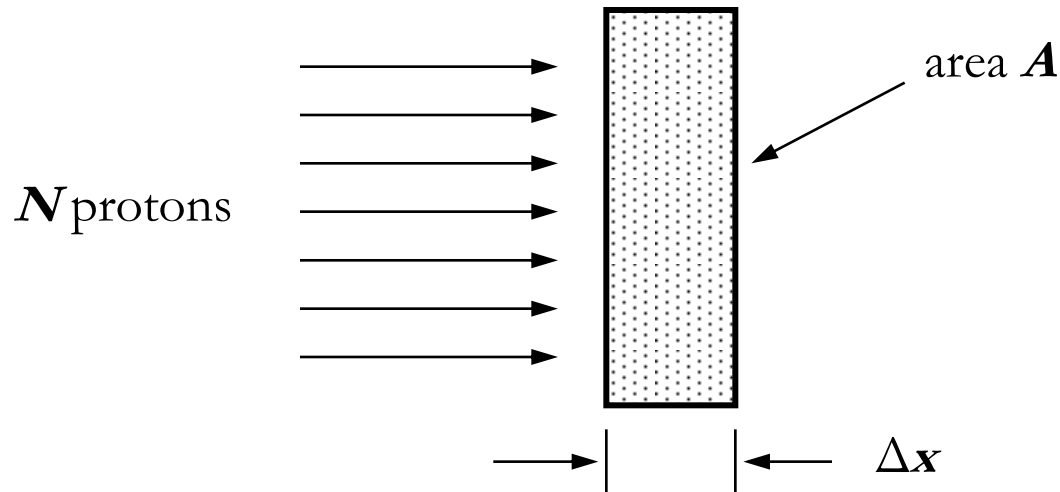
$$-\frac{dE}{dx} = \frac{4\pi n k^2 Z^2 e^4}{mc^2 b^2} \ln \frac{2mc^2 b^2}{I(1-b^2)} - b^2$$

$$\beta = v/c$$

$$\frac{S}{\rho} \equiv -\frac{1}{\rho} \frac{dE}{dx} \quad \frac{\text{Mev}}{\text{g/cm}^2}$$



# Protons/Ions – Basic Physics



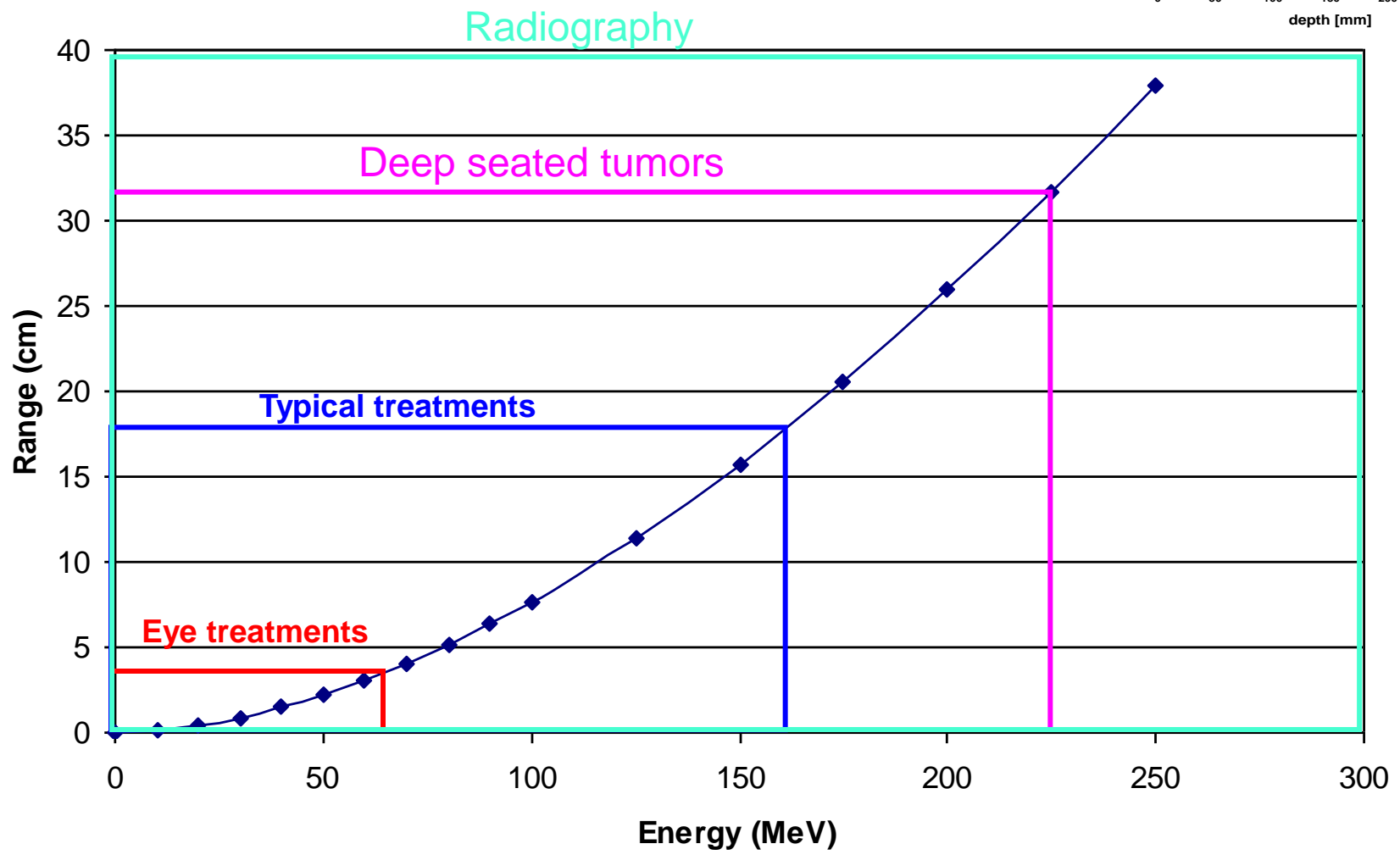
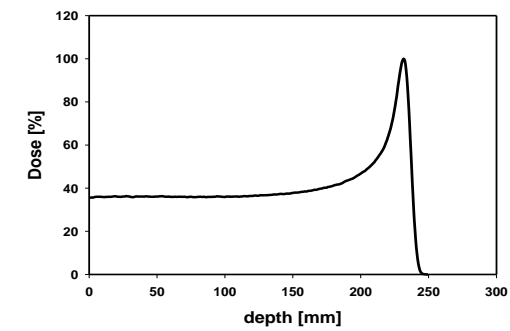
$$D \equiv \frac{\text{energy}}{\text{mass}} = \frac{(dE/dx) \times \Delta x \times N}{\rho \times A \times \Delta x} = \Phi \frac{S}{\rho}$$

Dose = fluence × mass stopping power

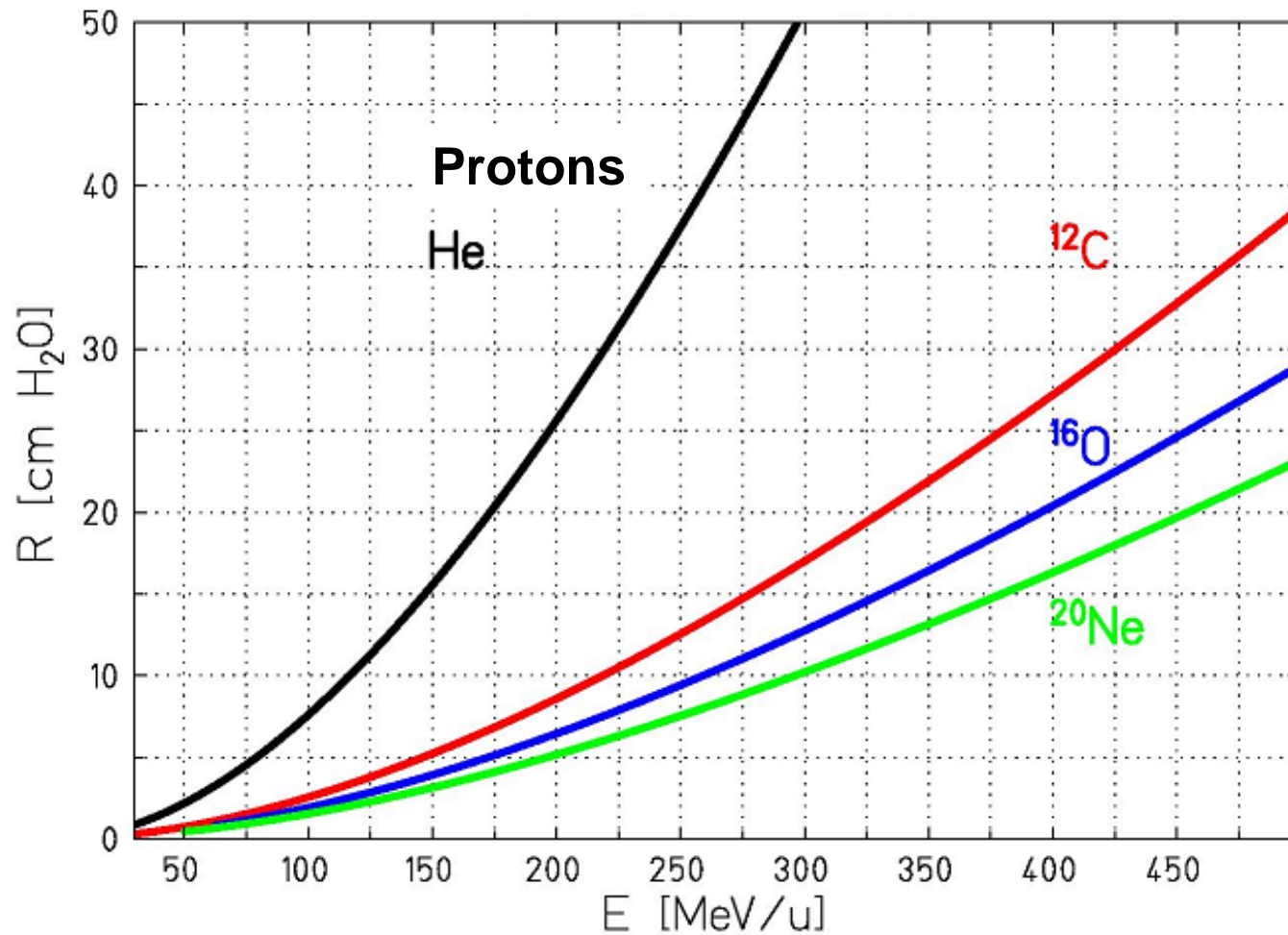


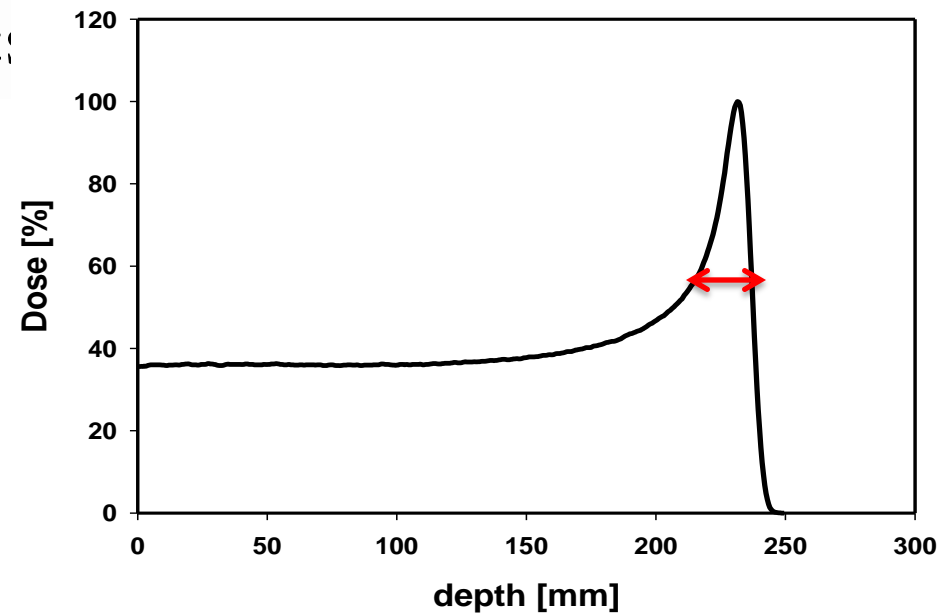


# Protons/Ions – Basic Physics



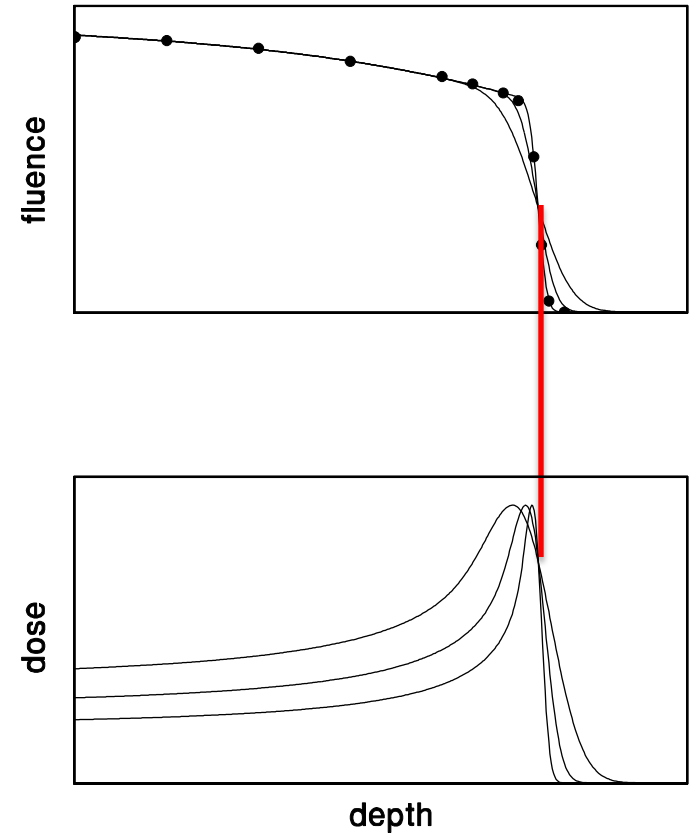
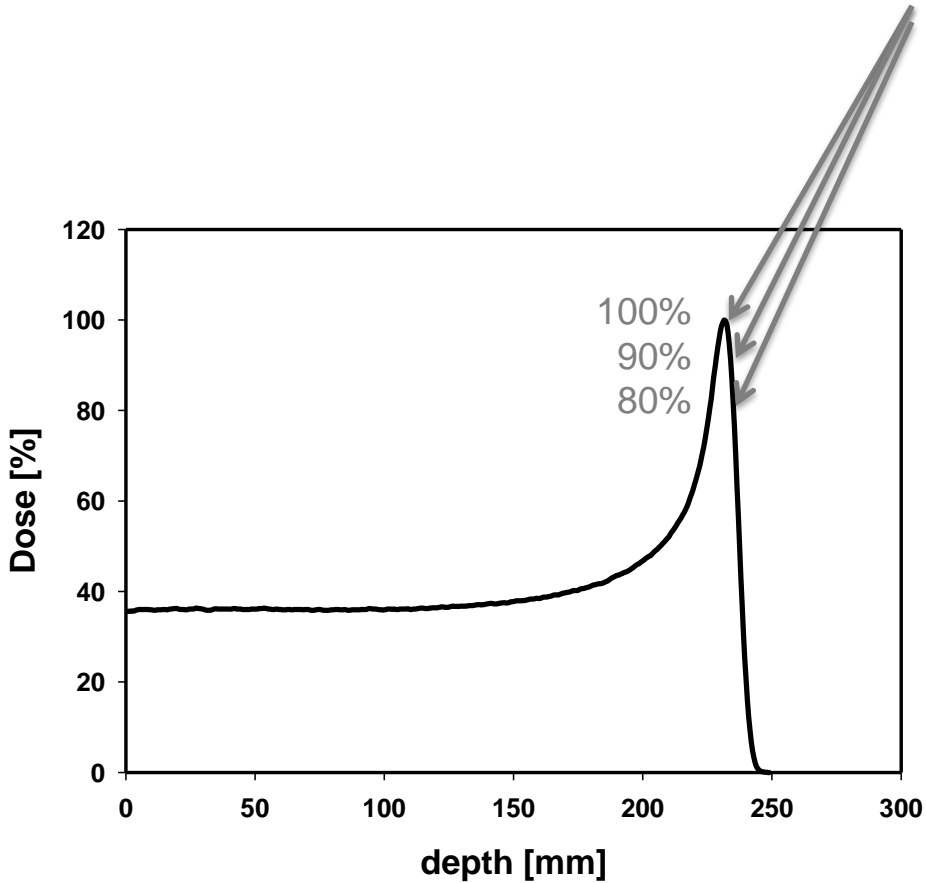
# Protons/Ions – Basic Physics





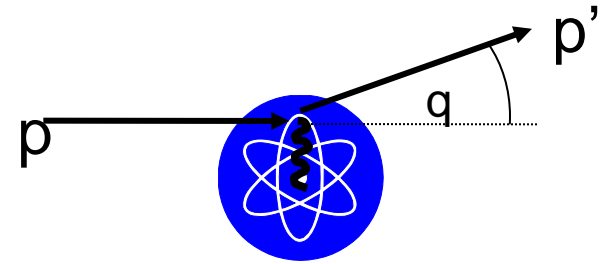
- Protons lose their energy in individual collisions with electrons
- Protons with the same initial energy may have slightly different ranges:  
“Range straggling”

## Beam Range

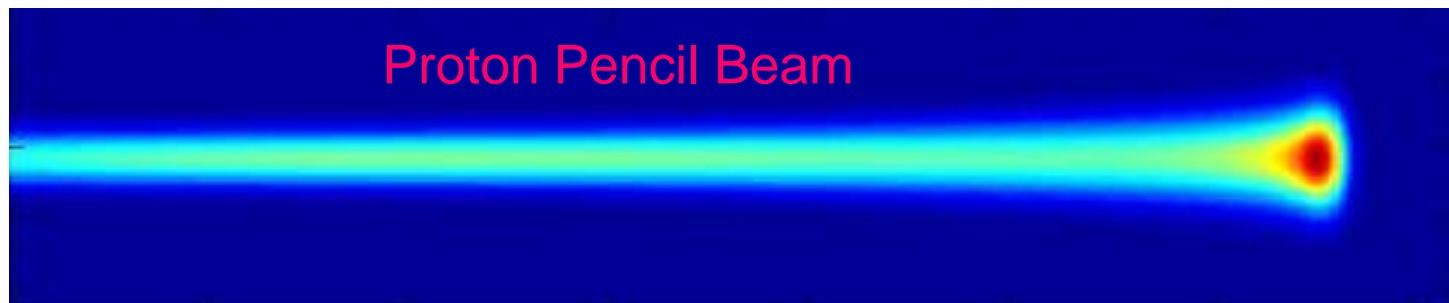


## Electromagnetic energy loss of protons

- Lateral distribution



Multiple Coulomb scattering (small angles)



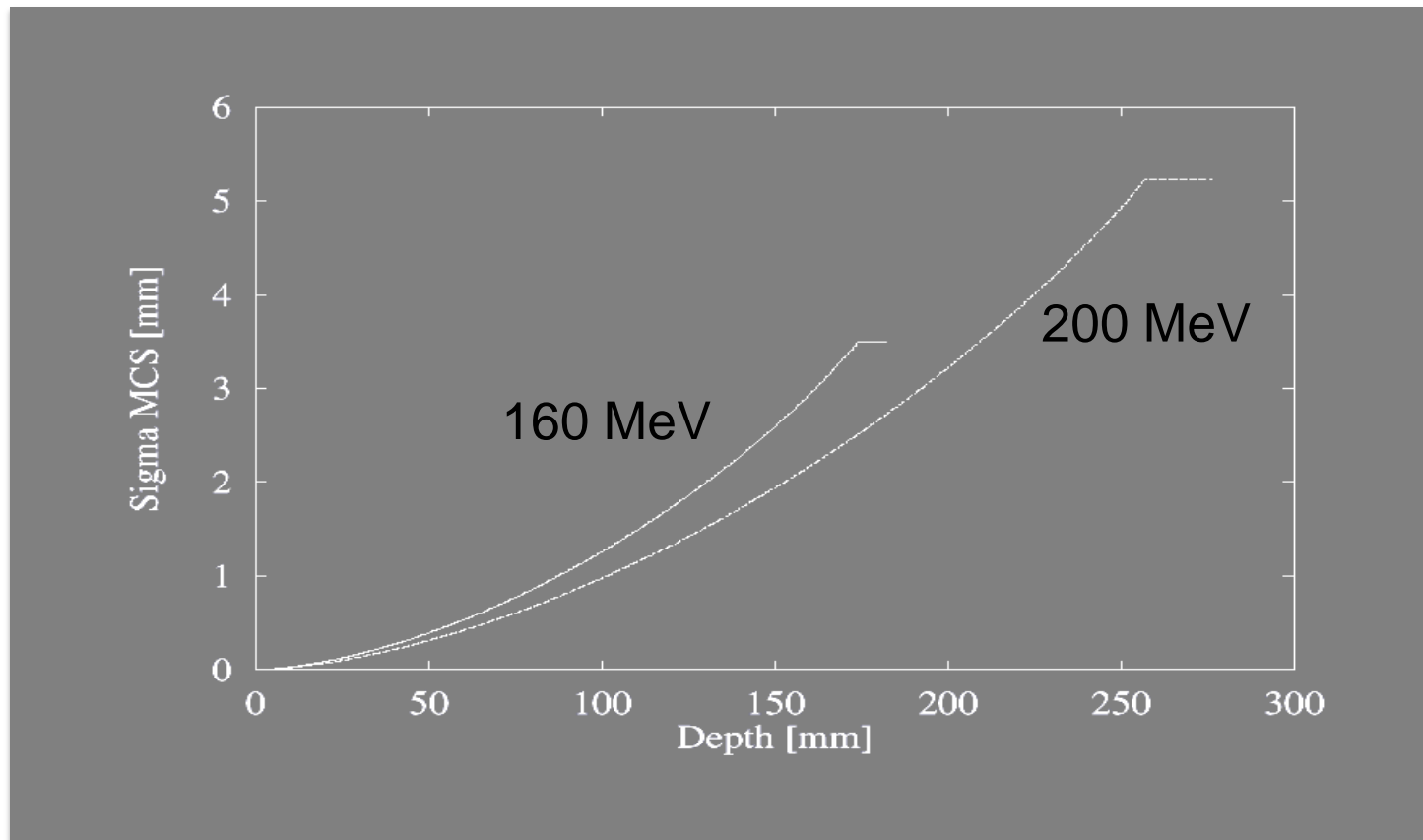
## Multiple Coulomb Scattering

- Protons are deflected in the electric field of the nuclei. In general, multiple deflections will occur
- For treatment planning related calculations a purely Gaussian approximation is a good approximation, except at the very end of the range

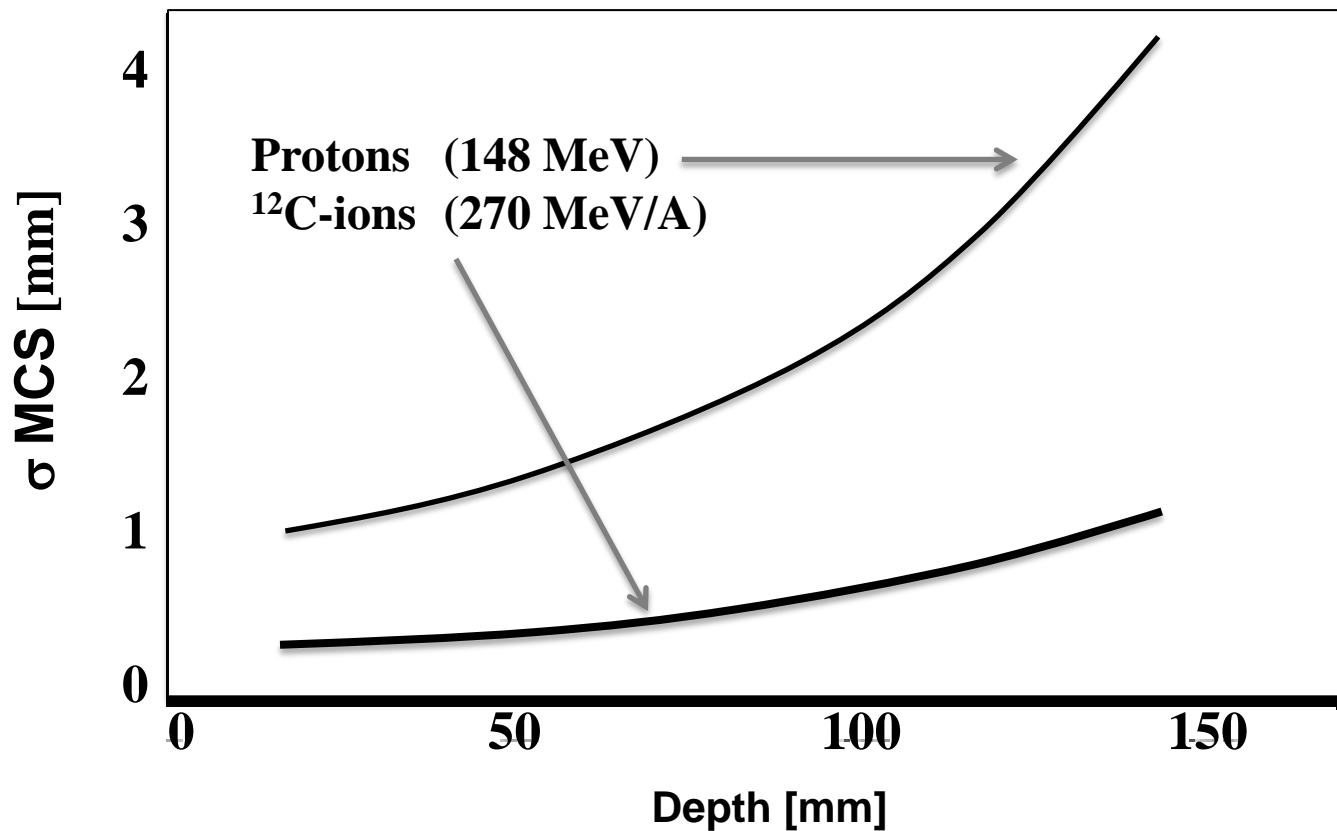




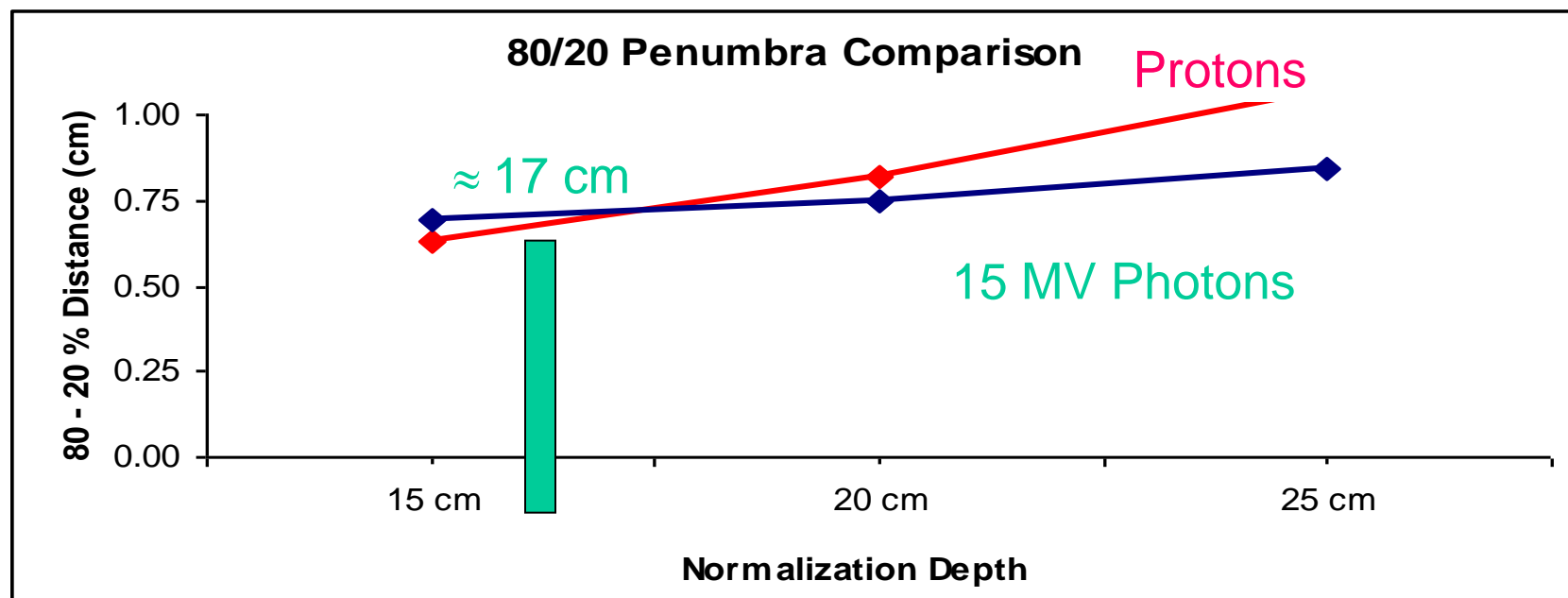
## Multiple Coulomb Scattering



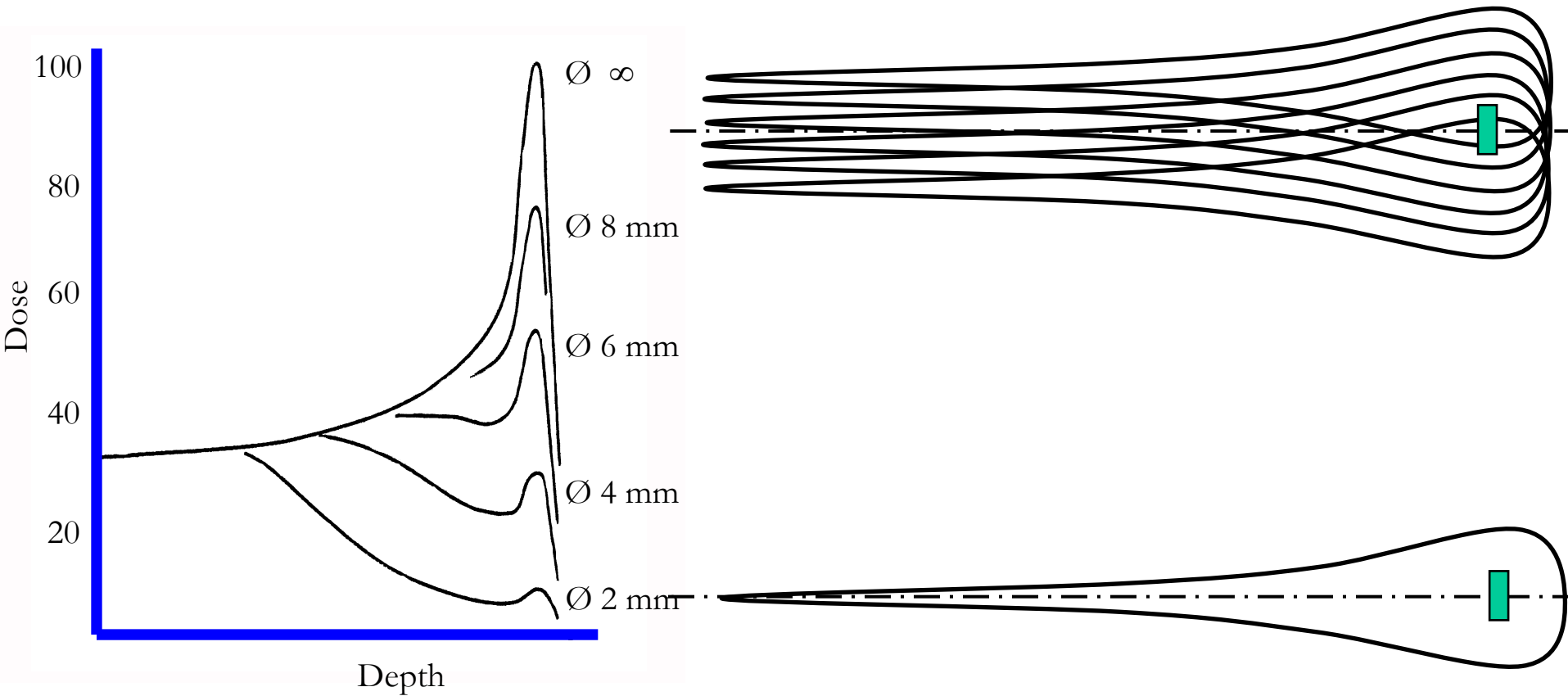
## Multiple Coulomb Scattering



## Multiple Coulomb Scattering



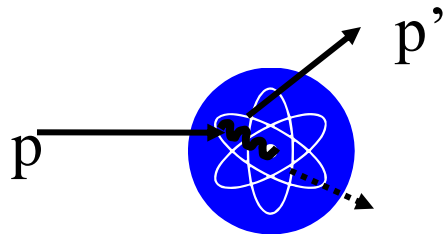
# Protons/Ions – Basic Physics



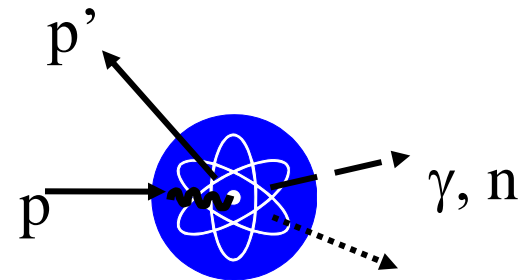
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## Nuclear interactions of protons



Elastic nuclear collision (large  $\theta$ )



Nuclear interaction



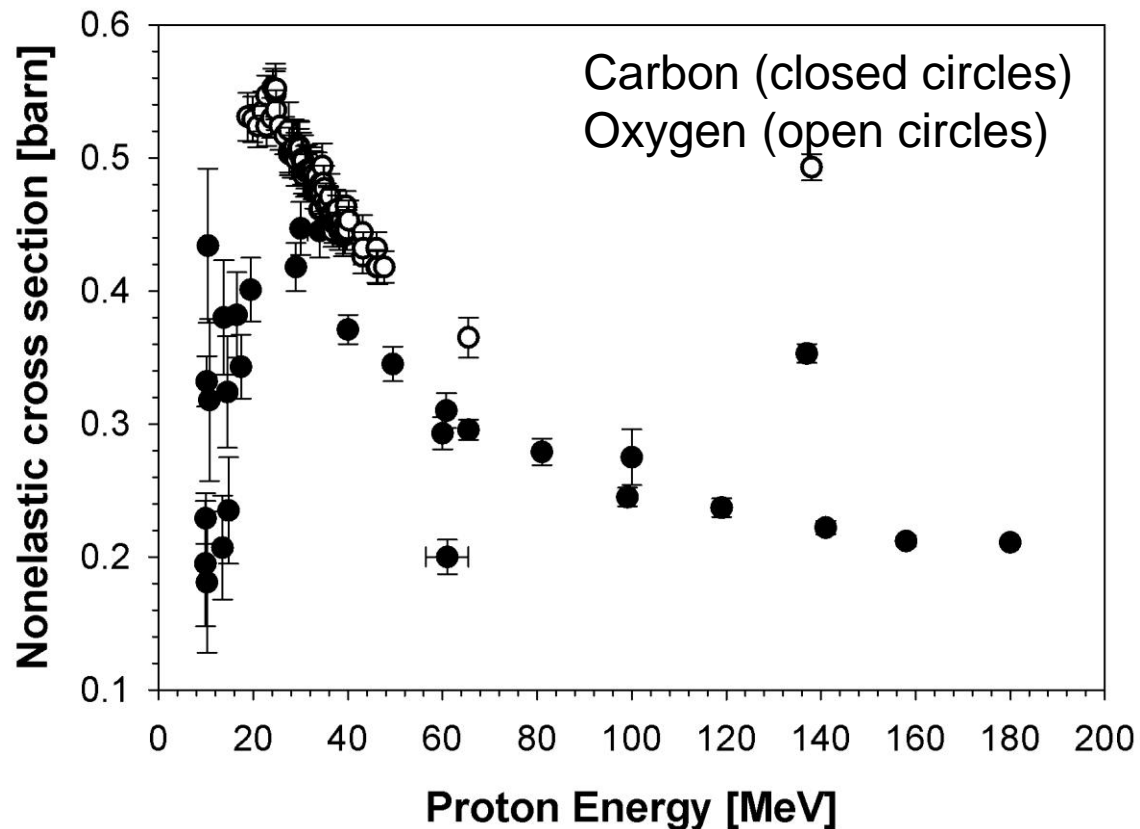
## Nuclear interactions of protons

- A certain fraction of protons have nuclear interactions in tissue, mainly with  $^{16}\text{O}$  (about 1% per cm of all protons)
- Nuclear interactions cause a decrease in primary proton fluence
- Nuclear interactions lead to secondary particles and thus to local and non-local dose deposition (neutrons!)
- The dose from nuclear interactions is negligible in the Bragg peak

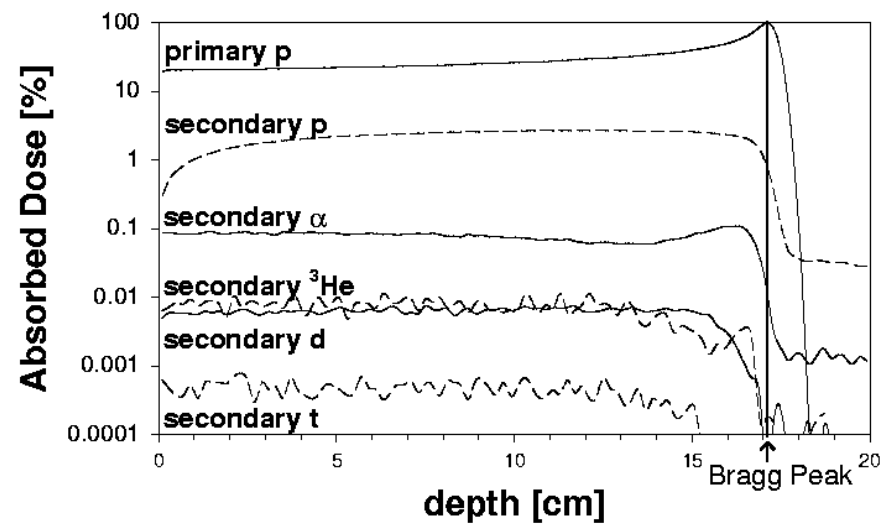
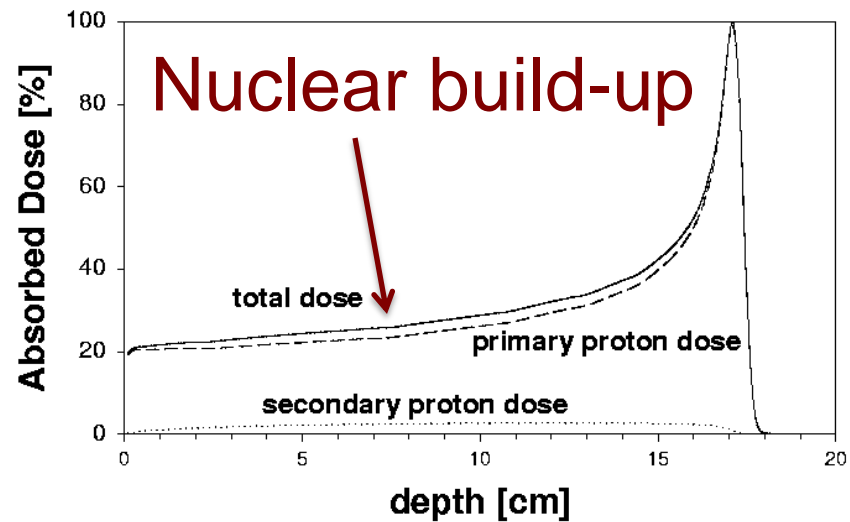
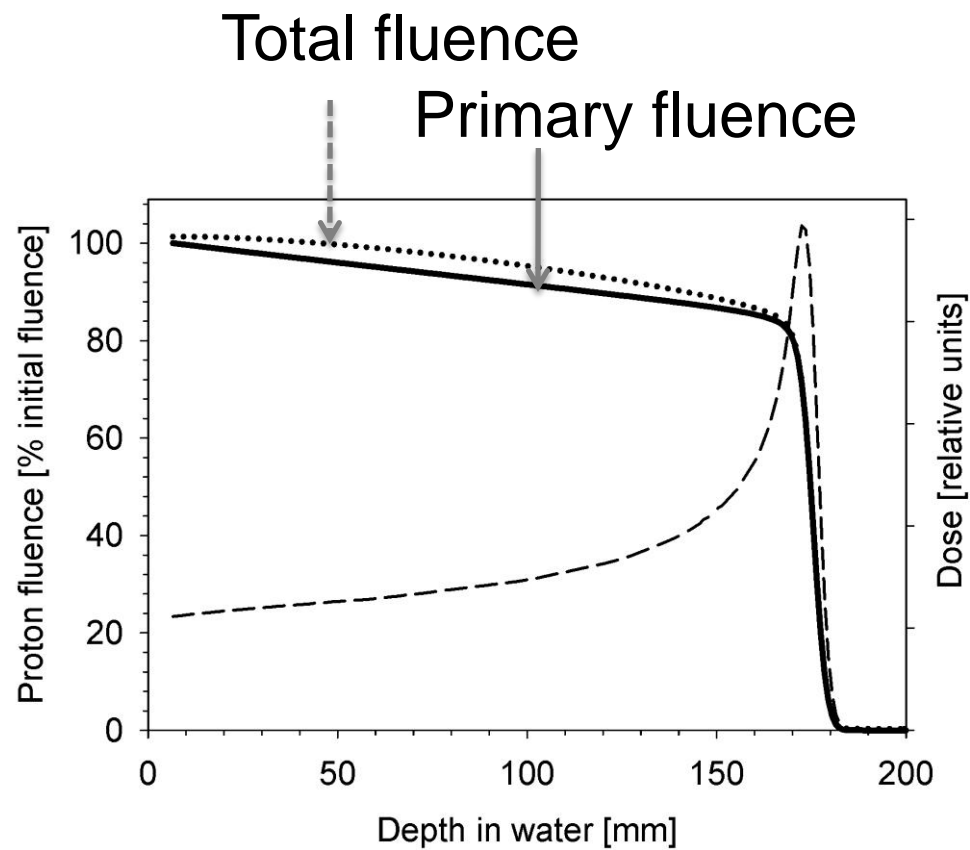




## Nuclear interactions of protons



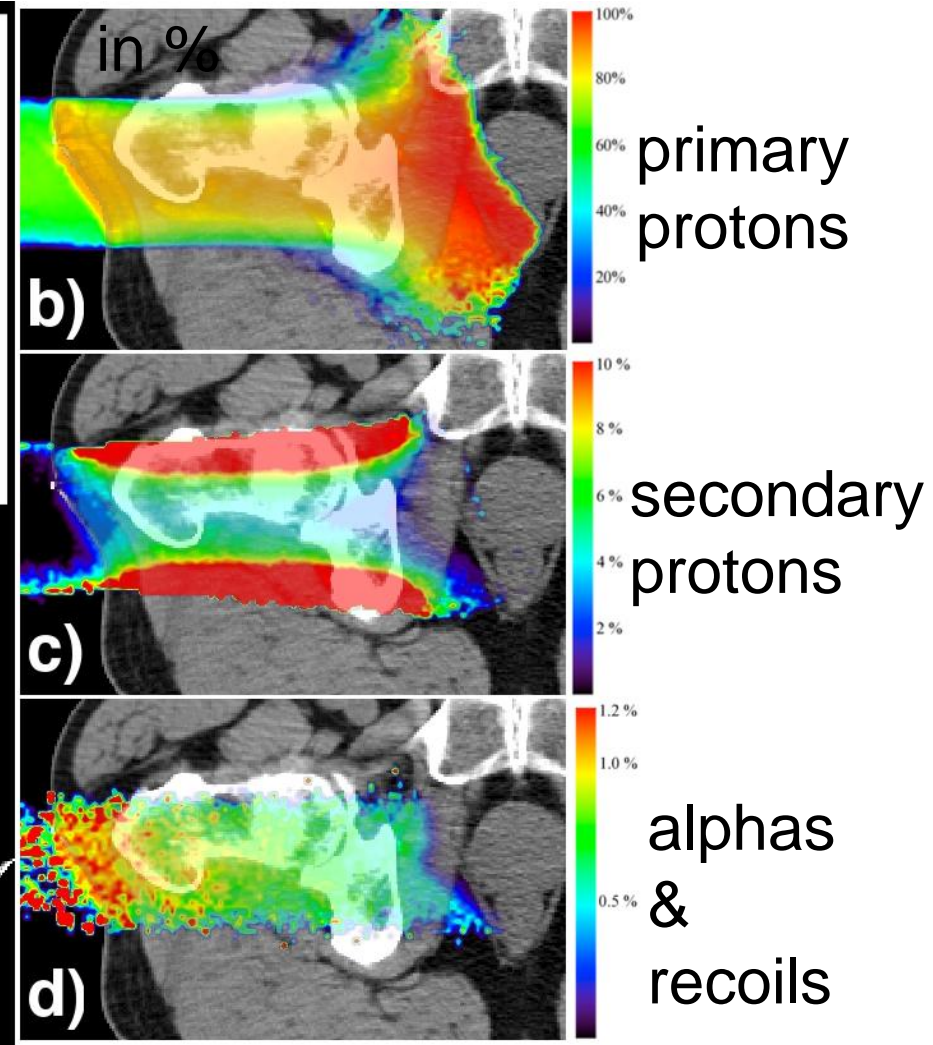
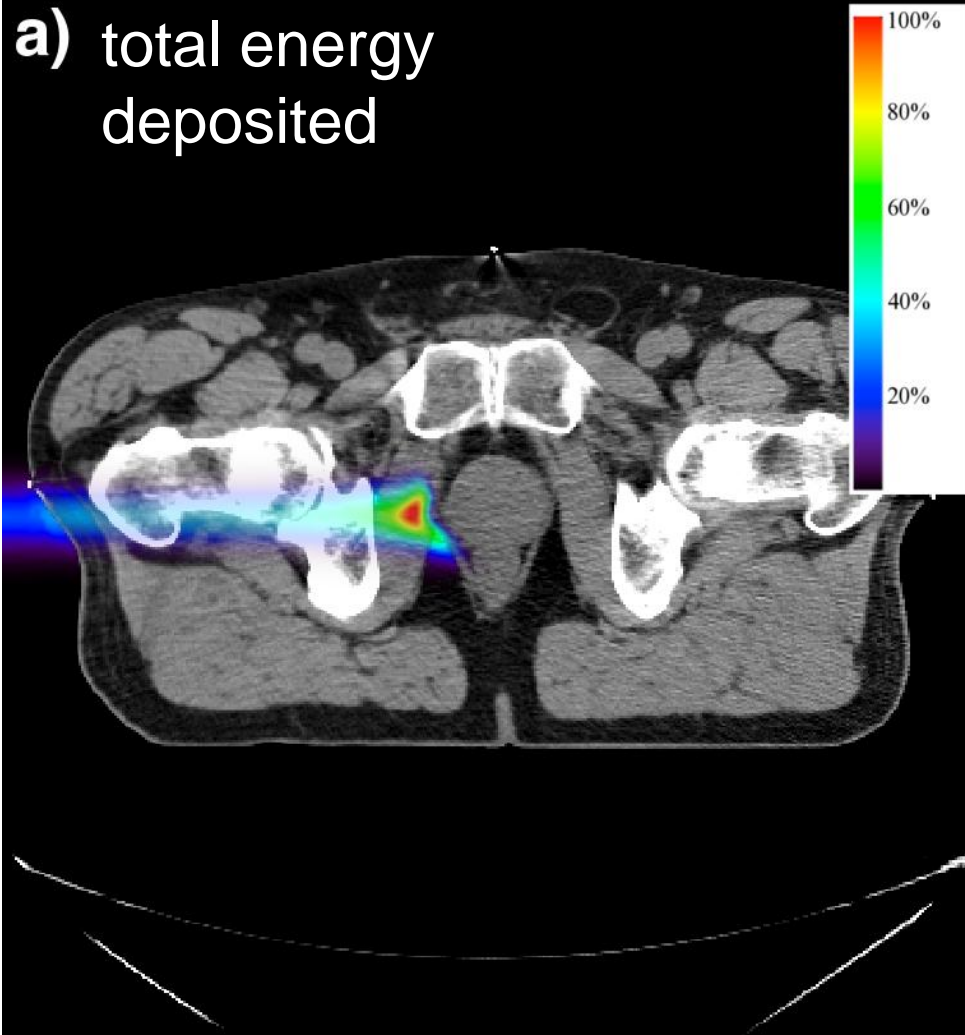
# Protons/Ions – Basic Physics



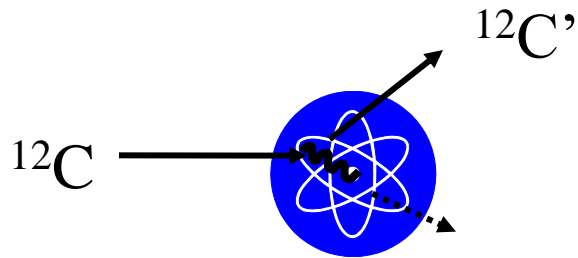
# Protons/Ions – Basic Physics

## Contribution

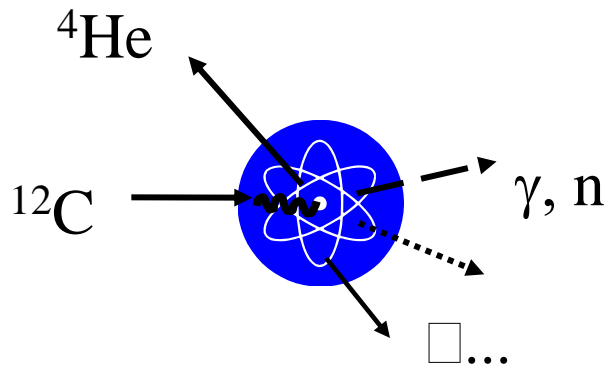
in %



## Nuclear interactions of heavy ions



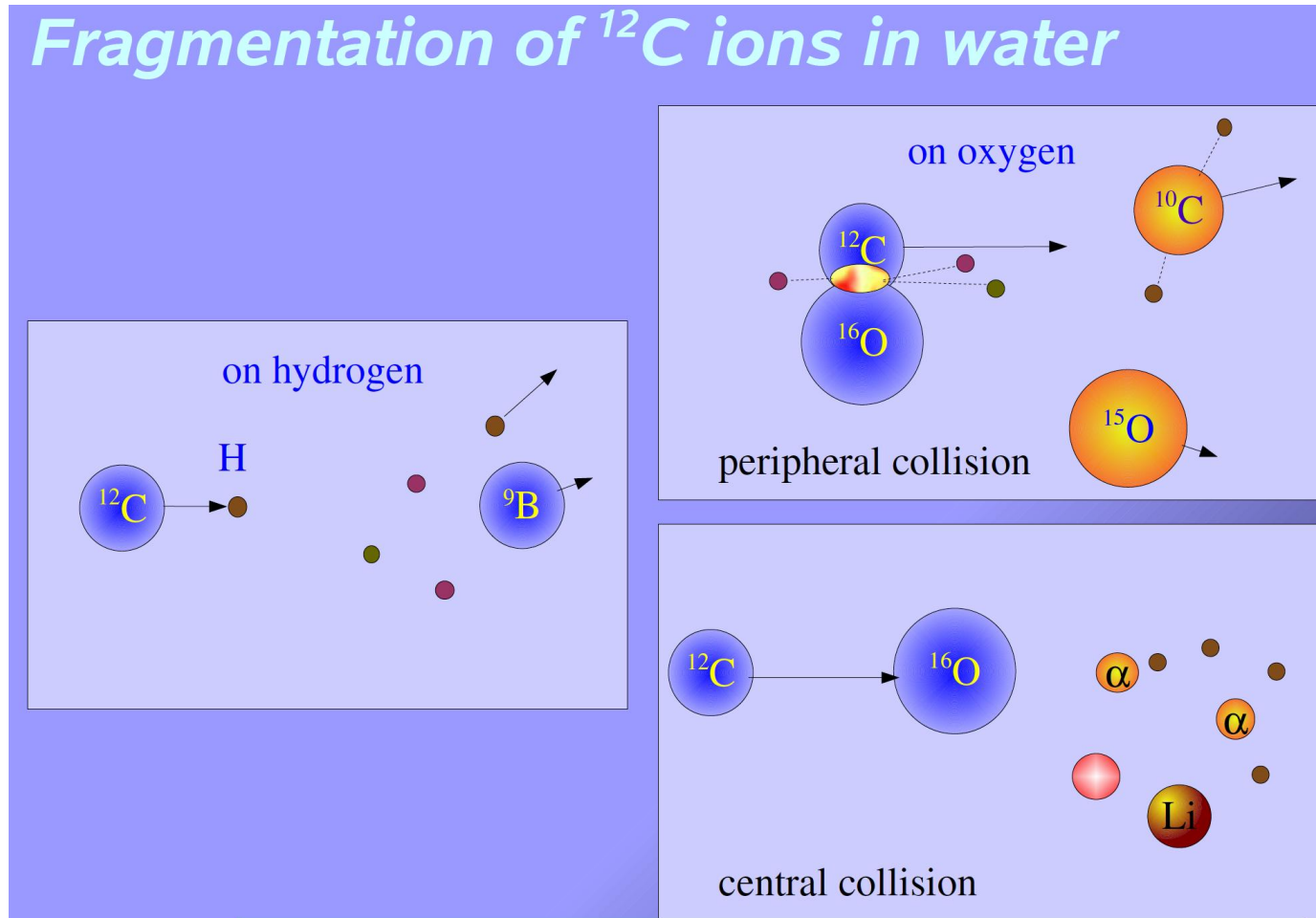
Elastic nuclear collision (large  $\theta$ )



Nuclear interaction (fragmentation)

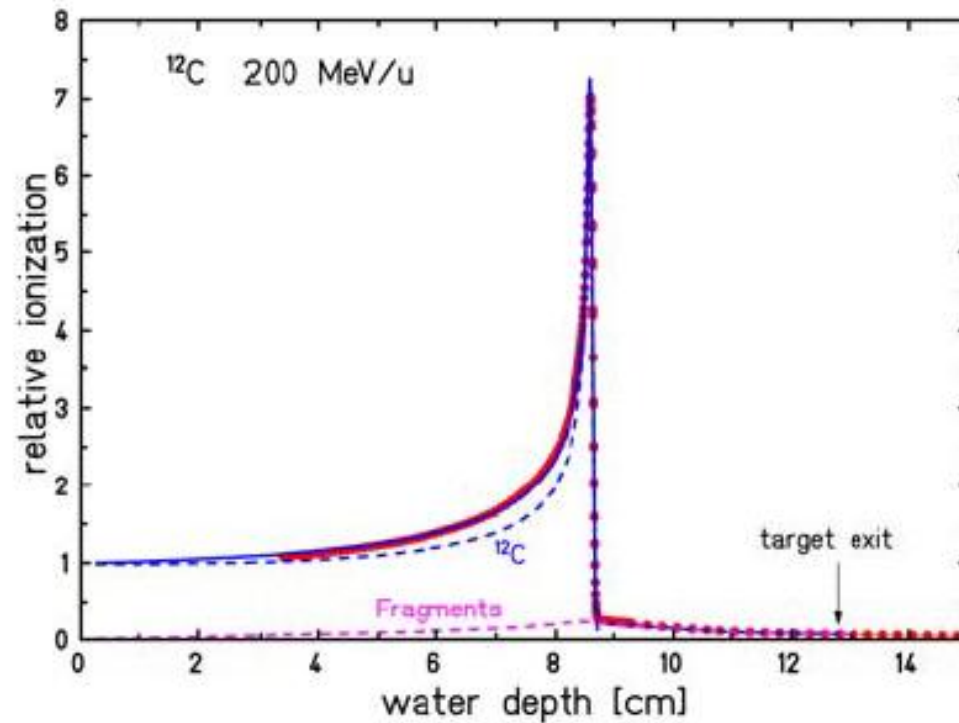


## Nuclear interactions of heavy ions

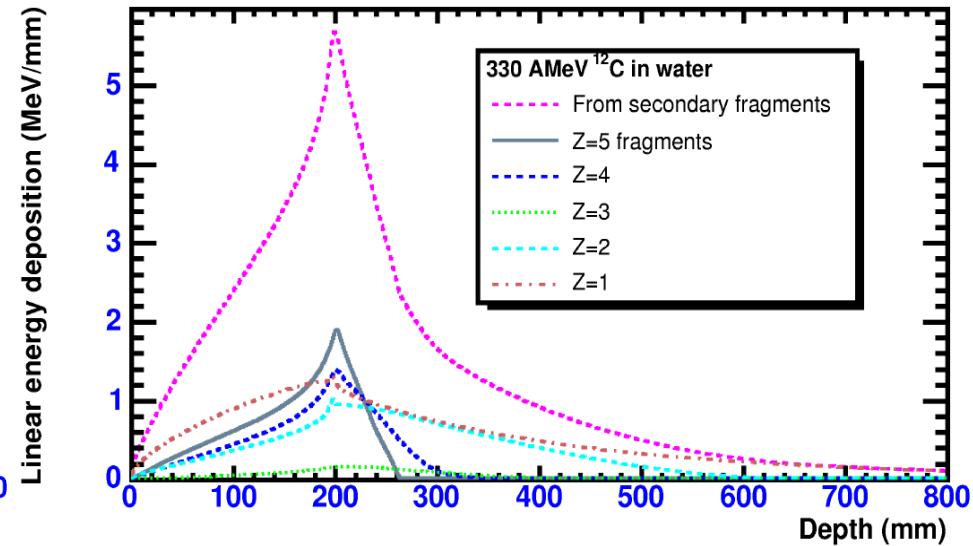
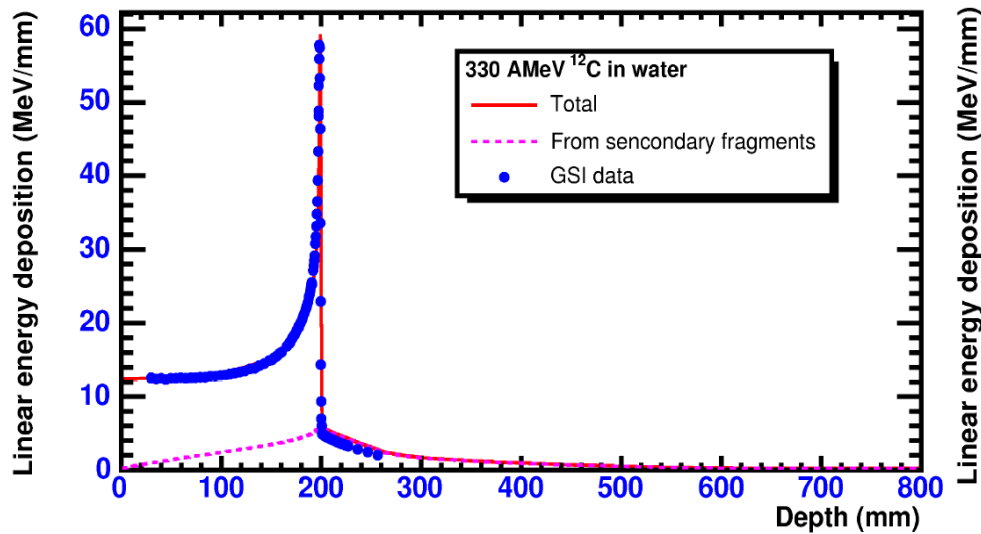


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## Nuclear interactions of heavy ions



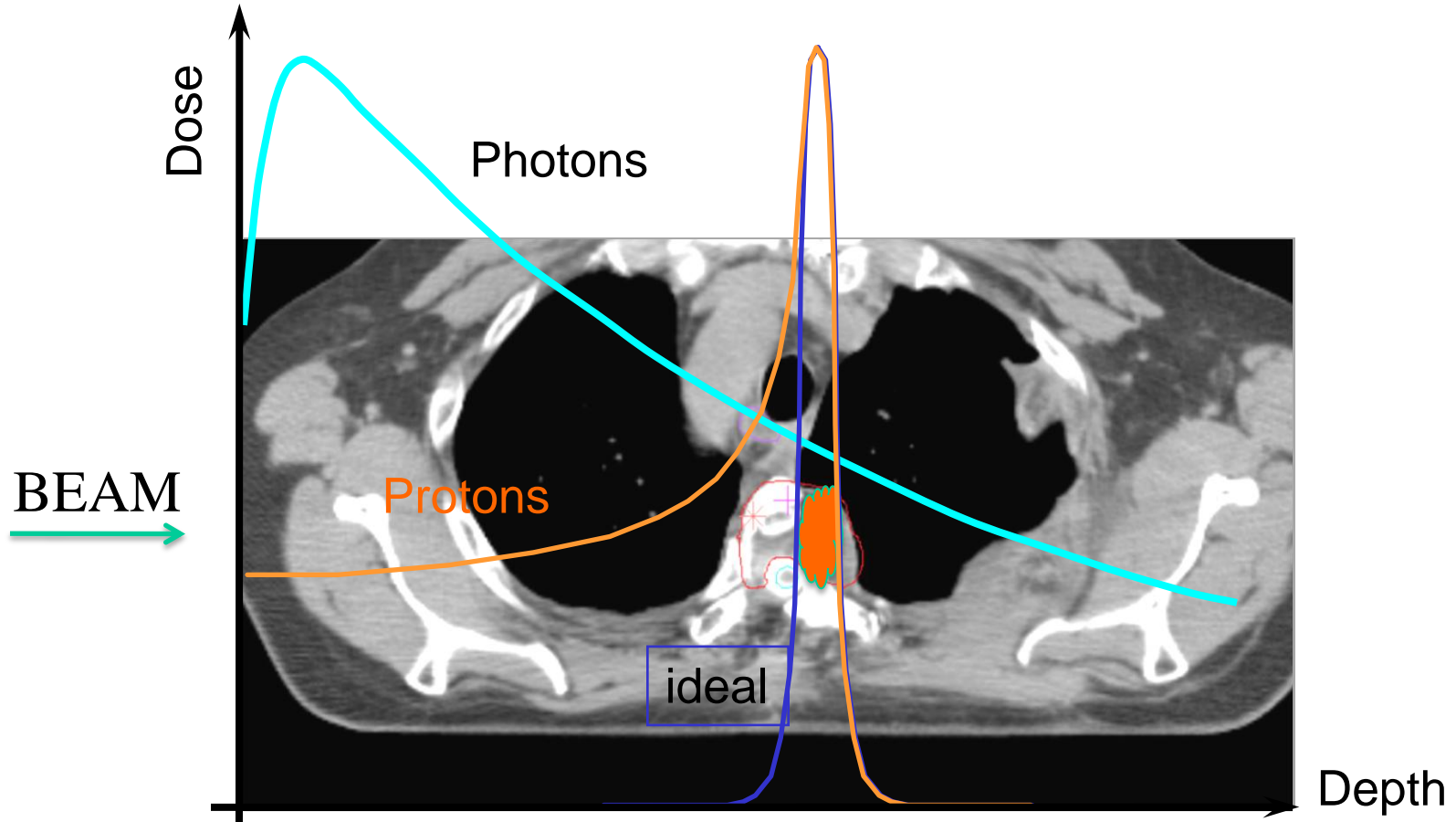
## Nuclear interactions of heavy ions



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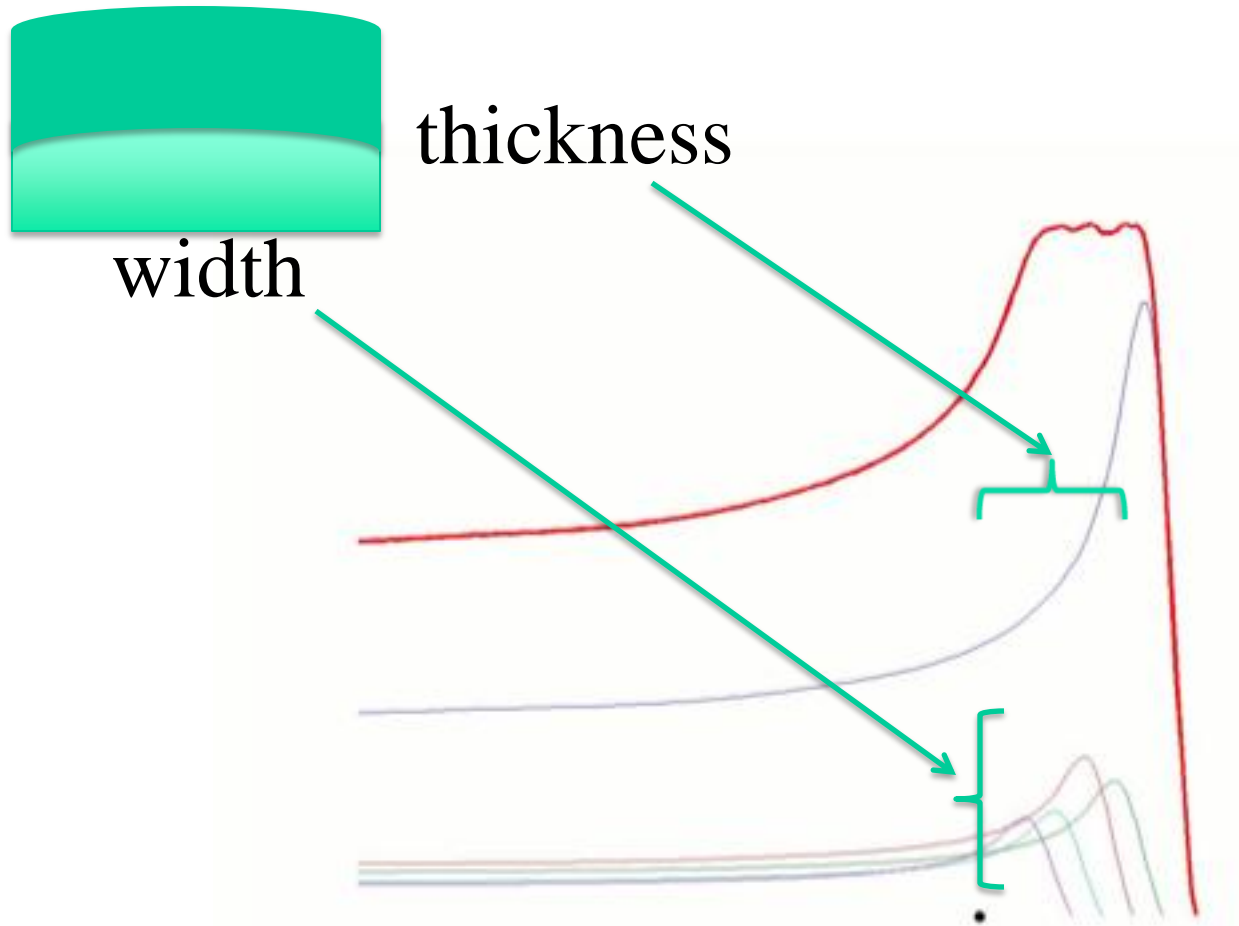


# Clinical dose distributions





# Clinical dose distributions



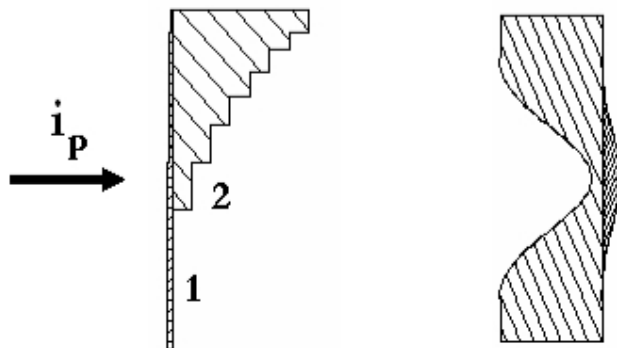
## Spread-out Bragg Peak



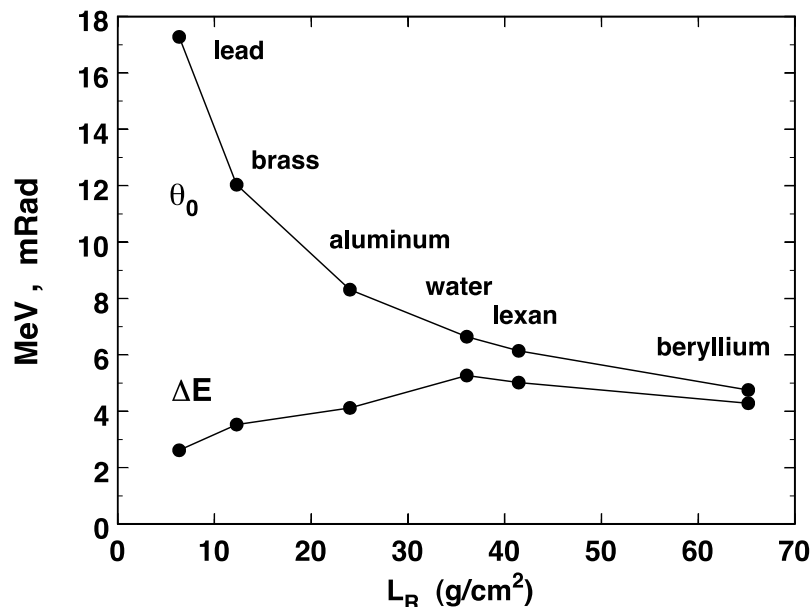
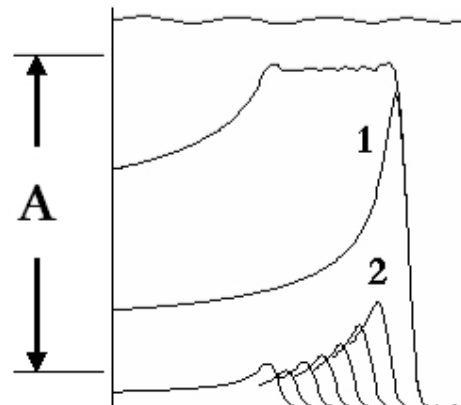
# Clinical dose distributions

RANGE MODULATOR

SECOND SCATTERER

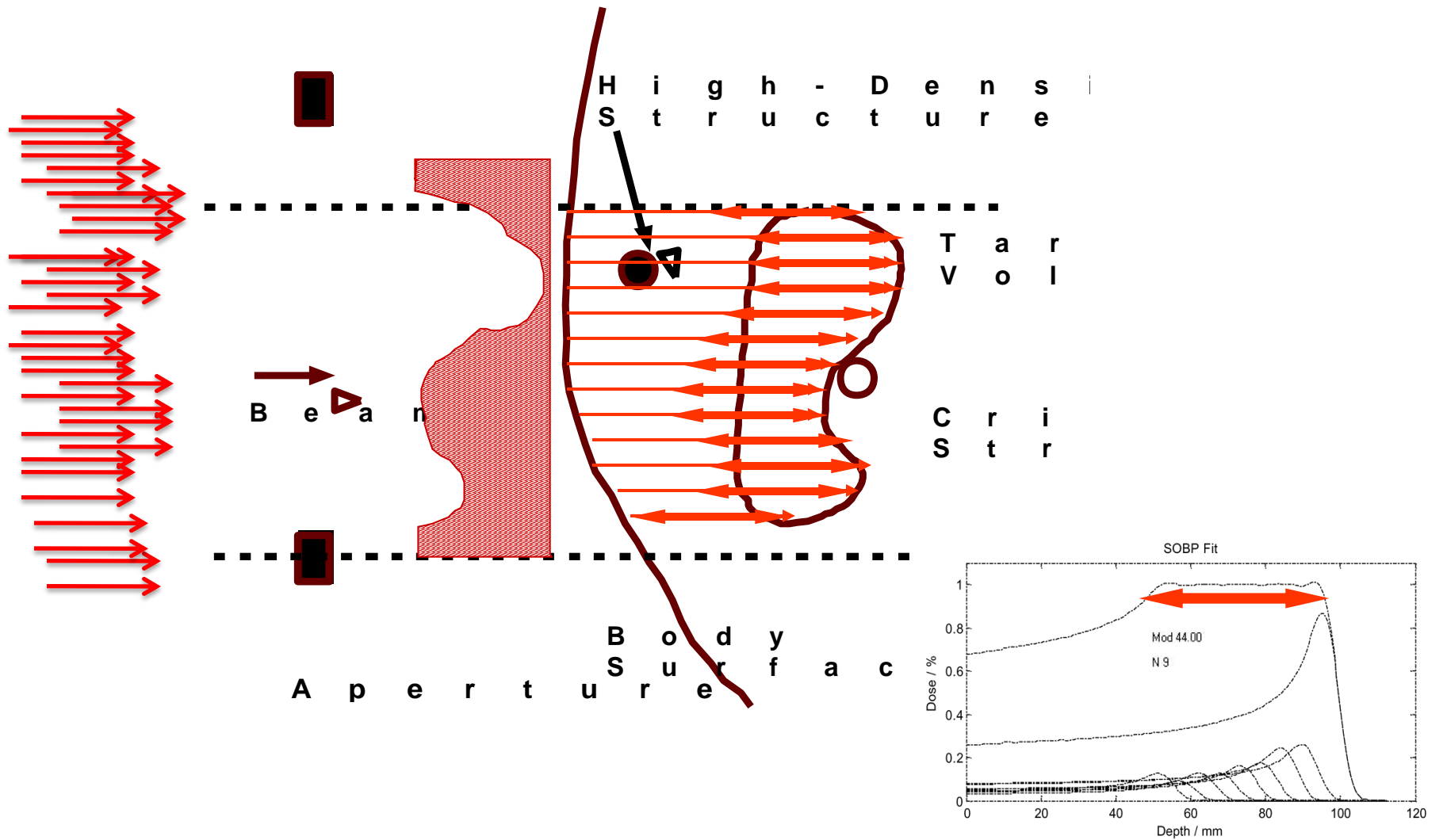


WATER TANK



Multiple scattering angle and energy loss for 160 MeV protons traversing 1 g/cm<sup>2</sup> of various materials

# Clinical dose distributions



# Take Home Messages

- Heavy charged particles interact very differently from photons (used in conventional radiation therapy)
- The most important interactions are ionization, Coulomb scattering, and non-elastic nuclear interactions
- Heavy charged particle treatments are associated with the reduction of the total energy deposited in the patient by more than a factor of 2

